

# On decomposing the Watson efficiency of ordinary least squares in a partitioned weakly singular linear model

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## Abstract

We consider the estimation of regression coefficients in a partitioned weakly singular linear model and focus on questions concerning the Watson efficiency of the ordinary least squares estimator of a subset of the parameters with respect to the best linear unbiased estimator. Certain submodels are also considered. The conditions under which the Watson efficiency in the full model splits into a function of some other Watson efficiencies is given special attention.

## Keywords

BLUE, efficiency multiplier, Frisch–Waugh–Lovell theorem, linear sufficiency, OLSE, reduced linear model, splitting the efficiency.

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